

MODERATE D
BASIC APPLIED MATHEMATICS
MARKING GUIDE

"
FORM-SIX INTERISLAMIC MOCK EXAMINATION

~~2024~~

YEAR - 2025

BASIC APPLIED MATHEMATICS MARKING SCHEME

FORM SIX INTER-ISLAMIC MOCK EXAMINATION

01. (a) (i) 0.0008 ✓

OR, 0.0548
(ii) = 21.4657

(0.2 marks)

(0.2 marks)

(0.2 marks)

(b) 1.5905

(0.2 marks)

(c) $\alpha = 0.0625 \text{ rad.}$

OR $3^\circ 35' 15'' = 3.58374928^\circ$

02. (a) $h(x) = \frac{x^2}{x^2-4} + \frac{1}{x+2}$

$= \frac{x^2+x-2}{x^2-4}$

$= \frac{(x+2)(x-1)}{(x-2)(x+2)} = \frac{x-1}{x-2}$

$\therefore h(x) = \frac{x-1}{x-2}$

$\frac{x^2(x+2)+x+2}{(x-2)(x+2)}$

$\frac{x^3+2x^2+x+2}{(x-2)(x+2)}$

$\frac{x^3+2x^2+x-2}{x^2-4}$

(0.2 marks)

(0.2 marks)

Vertical Asymptote, $x-2=0$

$x=2$

$x=2$ or -2

(0.2 marks)

Horizontal Asymptote,
Oblique

$h(x)=y = \frac{x-1}{x-2}$

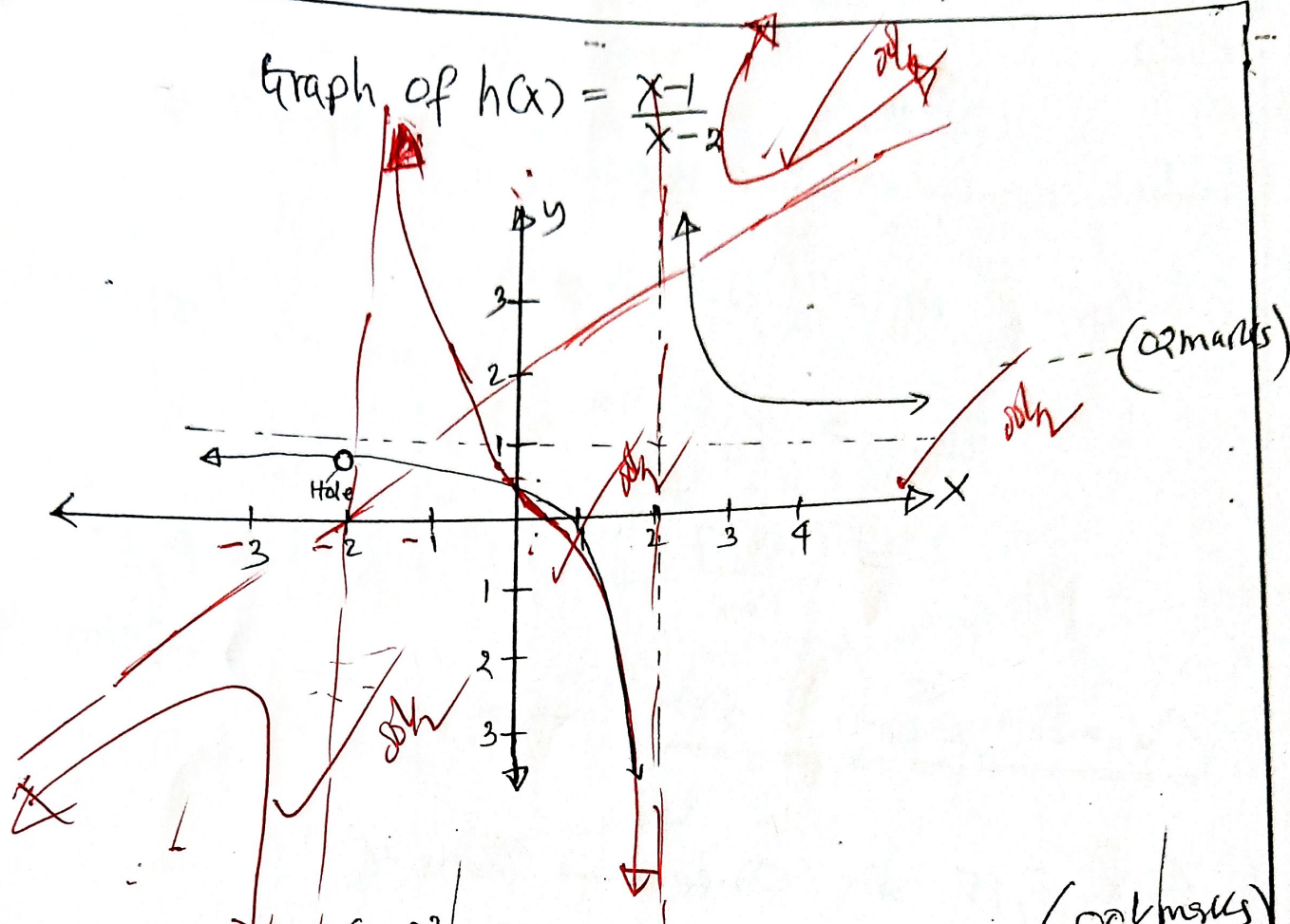
$y = \frac{x}{x} - \frac{1}{x}$
 $\frac{x}{x} - \frac{2}{x}$

$y = 1 - \frac{1}{x}$, $x \rightarrow \infty$, $\frac{1}{x} \approx 0$ and $\frac{2}{x} \approx 0$.

$y = 1 + 2$

(0.2 marks)

2@

Graph of $h(x) = \frac{x-1}{x-2}$ 

$$2 \text{ (b)(i) } g(x) = -2(x-1)^2 + 3$$

$$= -2(x^2 + 2x + 1) + 3$$

$$g(x) = -2x^2 + 4x + 1$$

$$\text{Turning point} = \left(-\frac{b}{2a}, \frac{4ac - b^2}{4a} \right)$$

$$= \left(\frac{-4}{2(-2)}, \frac{4(-2)(1) - 4^2}{4(-2)} \right)$$

$$\therefore \text{Turning point} = (1, 3)$$

(ii) Turning point is maximum.

$$(iii) \text{ Line of symmetry} = -\frac{b}{2a} = \frac{-4}{2(-2)} = 1$$

$$\therefore x = 1$$

$$(iv) \text{ Domain} = \{x; x \in \mathbb{R}\}$$

$$\text{Range} = y; y \geq \frac{4ac - b^2}{4a} = \frac{4(-2)(1) - 4^2}{4(-2)}$$

$$\therefore \text{Range} = y \geq 3$$

03 (a)

Solution

Let number of boys = B and number of girls = G

Given, $\frac{G}{B} = \frac{7}{12}$, but: $B = 1380$.

$$\frac{G}{1380} = \frac{7}{12}$$

$$G = \frac{1380 \times 7}{12}$$

Number of girls is 805

(b) 6, X, y, 15 are consecutive terms of AP

$$A_2 - A_1 = A_3 - A_2 = A_4 - A_3$$

$$\text{from } A_2 - A_1 = A_3 - A_2$$

$$X - 6 = y - X$$

$$2X - y = 6 \quad \text{--- (i)}$$

$$\text{then } A_3 - A_2 = A_4 - A_3$$

$$y - X = 15 - y$$

$$2y - X = 15 \quad \text{--- (ii)}$$

Solve eqn (i) and (ii) Simultaneously

$$\therefore \underline{X = 9 \text{ and } y = 12}$$

Required, $A_n = ?$ from, $A_n = A_1 + (n-1)d$, but $A_1 = 6$, $d = 9 - 6 = 3$

$$A_n = 6 + (n-1) \times 3$$

$$= 6 + 3n - 3$$

$$\therefore \underline{A_n = 6 - 3 + 3n = 3 + 3n}$$

Solution;
 let "t" be the number of typists.
 "p" be the number of pages.
 "d" be the number of days.

Then $t \propto \frac{p}{d}$ ----- (0/1 mark)

$$t = \frac{kp}{d} \Rightarrow \frac{td}{p} = k \text{ ----- (0/1 mark)}$$

$$\frac{t_1 d_1}{p_1} = \frac{t_2 d_2}{p_2}, \text{ But } t_1 = 2, d_1 = 3, p_1 = 210$$

$$d_2 = 2, p_2 = 700, t_2 = ?$$

$$\frac{2 \times 3}{210} = \frac{2t}{700} \Rightarrow t = \frac{2 \times 3 \times 700}{2 \times 210} = 10 \text{ typists. ----- (0/1 mark)}$$

$\therefore$ 10 typists will be needed to type 700 pages in 2 days.

(a)(i) $f(x) = \frac{x^2}{x-1}$
 $f(x+h) = \frac{(x+h)^2}{(x+h)-1}$

From first principle;

$$f'(x) = \lim_{h \rightarrow 0} \frac{f(x+h) - f(x)}{h} \text{ ----- (0/1 mark)}$$

$$= \lim_{h \rightarrow 0} \left(\frac{(x+h)^2}{x+h-1} - \frac{x^2}{x-1} \right) \text{ ----- (0/1 mark)}$$

$$= \lim_{h \rightarrow 0} \left(\frac{x^3 + 2x^2h + xh^2 - x^2 - 2xh - h^2 - x^3 - x^2h + x^2}{h(x-1)(x+h-1)} \right) \text{ ----- (0/1 mark)}$$

$$= \lim_{h \rightarrow 0} \left(h \frac{x^2 - 2x - h}{h(x-1)(x+h-1)} \right) = \frac{x^2 - 2x}{(x-1)(x-1)}$$

$$\therefore f'(x) = \frac{x^2 - 2x}{(x-1)^2} \text{ ----- (0/1 mark)}$$

f (a)(ii) Given $g(x) = x \cos x$
Required, $g'(x) = ?$

from: Product Rule:

$$g'(x) = v \frac{du}{dx} + u \frac{dv}{dx}$$

$$\text{let } u = x \Rightarrow \frac{du}{dx} = 1$$

$$v = \cos x \Rightarrow \frac{dv}{dx} = -\sin x$$

$$g'(x) = \cos x + (x)(-\sin x)$$

$$\therefore \underline{g'(x) = \cos x - x \sin x}$$

(b) - Solution;

$$\text{Given } A = 4\pi r^2$$

$$r = 40 \text{ cm and } \frac{dr}{dt} = 0.1 \text{ cm/s}$$

$$\Rightarrow \frac{dA}{dt} = 8\pi r \frac{dr}{dt}$$

$$\frac{dA}{dt} = 8\pi (40) \times 0.1 \text{ cm}^2/\text{s}$$
$$= 32\pi \text{ cm}^2/\text{s}$$

$$\frac{dA}{dt} = 32\pi \text{ cm}^2/\text{s}$$

$\therefore$ Rate of change of the area is $32\pi \text{ cm}^2/\text{s}$.

Solution;

$$\begin{aligned} \text{(i)} \quad \int_1^2 (9x^3 - 4x) dx &= 9 \int_1^2 x^3 dx - 4 \int_1^2 x dx \\ &= \left(\frac{9x^4}{4} - 2x^2 \right) \Big|_1^2 \quad \text{--- (0/mark)} \\ &= \left(\frac{9(2)^4}{4} - 2(2)^2 \right) - \left(\frac{9(1)^4}{4} - 2(1)^2 \right) \quad \text{--- (0/mark)} \\ &= \frac{111}{4} \text{ or } 27.75. \end{aligned}$$

$$\therefore \int_1^2 (9x^3 - 4x) dx = \frac{111}{4} \quad \text{--- (0/mark)}$$

$$\begin{aligned} \text{(ii)} \quad \int \frac{\sqrt{x^3} - 4}{x^2} dx &= \int \left(\frac{\sqrt{x^3}}{x^2} - \frac{4}{x^2} \right) dx \\ &= \int \left(x^{\frac{1}{2}} - 4x^{-2} \right) dx \quad \text{--- (0/marks)} \\ &= \frac{x^{\frac{1}{2}+1}}{\frac{1}{2}+1} - \frac{4x^{-2+1}}{-2+1} + C \quad \text{--- (0/marks)} \\ &= 2x^{\frac{3}{2}} + \frac{4}{x} + C \\ &= 2\sqrt{x^3} + \frac{4}{x} + C \end{aligned}$$

$$\therefore \int \frac{\sqrt{x^3} - 4}{x^2} dx = 2\sqrt{x^3} + \frac{4}{x} + C \quad \text{--- (0/mark)}$$

(b) From the graph; The roots of $f(x)$ are $x = -1$ and $x = 1$

$$\text{Then } f(x) = (x-1)(x+1)$$

$$f(x) = x^2 - 1$$

----- (0/1 mark)

Area under the curve is given by

$$A = \int_a^b y dx.$$

$$\text{Area} = \int_0^1 (x^2 - 1) dx + \int_1^2 (x^2 - 1) dx$$

----- (0/1 mark)

$$= \left(\frac{x^3}{3} - x \right) \Big|_0^1 + \left[\frac{x^3}{3} - x \right] \Big|_1^2$$

$$A = \left(\frac{1}{3} - 1 - 0 \right) + \left(\left(\frac{8}{3} - 2 \right) - \left(\frac{1}{3} - 1 \right) \right)$$

----- (0/1 mark)

$$\text{Area} = \frac{2}{3} + \frac{4}{3} = 2.$$

$\therefore$ Area under curve is 2 sq. units

----- (0/1 mark)

Solution;

06 (a) Frequency Distribution table.

class Interval	Frequency
11 - 20	1
21 - 30	3
31 - 40	4
41 - 50	10
51 - 60	4
61 - 70	2
71 - 80	2
81 - 90	4

----- (03 marks)

(1) $A = 60$

C.I	f	X	$d = X - 60$	d^2	fd	fd^2
11-20	1	15.5	-44.5	1980.25	-44.5	1980.25
21-30	3	25.5	-34.5	1190.25	-103.5	3570.75
31-40	4	35.5	-24.5	600.25	-98	2401
41-50	10	45.5	-14.5	210.25	-145	2102.5
51-60	4	55.5	-4.5	20.25	-18	81
61-70	2	65.5	5.5	30.25	11	60.5
71-80	2	75.5	15.5	240.25	31	480.5
81-90	4	85.5	25.5	650.25	102	2601
$\Sigma f(\Sigma)$	30				-265	13277.5
					00½ mark	00½ mark
					01 mark	08½ mark
						01 mark

(i) standard deviation, $\sigma = \sqrt{\frac{\Sigma fd^2}{N} - \left(\frac{\Sigma fd}{N}\right)^2}$ ----- (00½ mark)

$\sigma = \sqrt{\frac{13277.5}{30} - \left(\frac{265}{30}\right)^2}$ ----- (01 mark)

S.D = 19.09333799

(ii) Median $= L + \left(\frac{\frac{N}{2} - \Sigma f_b}{f_w}\right) \times C$ ----- (00½ mark)

Median class is 41-40, since $\frac{N}{2} = 15$

Median $= 40.5 + \left(\frac{15 - 8}{10}\right) \times 10$ ----- (01 mark)

Median $= 47.5$ ----- (00½ mark)

Solution

Verify $\frac{3}{7}({}^8C_3 + {}^8C_2) = {}^9C_2$.

Since ${}^nC_r = \frac{n!}{(n-r)!r!}$

$$\frac{3}{7} \left(\frac{8!}{(8-3)!3!} + \frac{8!}{(8-2)!2!} \right) = \frac{9!}{(9-2)!2!} \text{ --- (0/mark)}$$

$$\frac{3}{7} \left(\frac{8!}{5!3!} + \frac{8!}{6!2!} \right) = \frac{9!}{7!2!}$$

$$\frac{3 \times 8!}{7 \times 5!2!} \left(\frac{1}{3} + \frac{1}{6} \right) = \frac{9 \times 8!}{7!2!} \text{ --- (0/mark)}$$

$$\frac{9 \times 8!}{7 \times 6 \times 5!2!} = \frac{9 \times 8!}{7!2!}$$

$$\frac{9!}{7!2!} = \frac{9!}{7!2!} \text{ --- (0/mark)}$$

Since L.H.S = R.H.S

Hence, verified that $\frac{3}{7}({}^8C_3 + {}^8C_2) = {}^9C_2$

(i) Solution;

Given $P(A) = \frac{1}{3}$, $P(B) = \frac{2}{7}$

$P(A \cup B) = ?$ If A and B are mutually exclusive, $P(A \cap B) = 0$.

from $P(A \cup B) = P(A) + P(B)$. ----- (0/1 mark)

$$P(A \cup B) = \frac{1}{3} + \frac{2}{7} = \frac{13}{21}$$

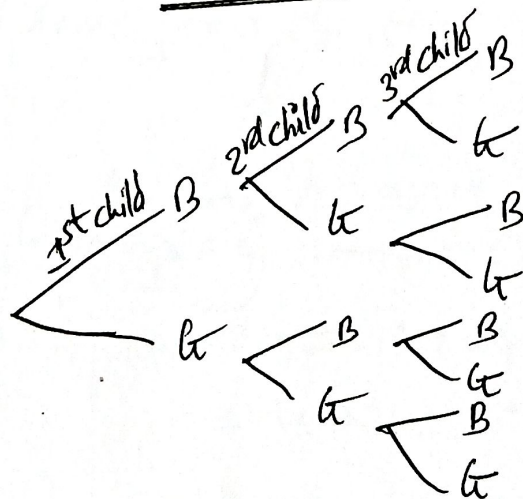
$\therefore P(A \cup B) = \frac{13}{21}$ ----- (00 1/2 mark)

(ii) If A and B are independent events.

$$P(A \cap B) = P(A) \times P(B)$$

$$P(A \cap B) = \frac{1}{3} \times \frac{2}{7} = \frac{2}{21}$$

$\therefore P(A \cap B) = \frac{2}{21}$ ----- (00 1/2 mark)



$S = \{BBB, BBG, BGB, BGG, GBB, GBG, GGB, GGG\} \Rightarrow n(S) = 8$

$E = \text{one boy and two girls} = \{BBG, GBG, GGB\} \Rightarrow n(E) = 3$ ----- (0/1 mark)

From, $P(E) = \frac{n(E)}{n(S)} = \frac{3}{8}$ ----- (0/1 mark)

$$P(E) = \frac{3}{8}$$

$\therefore$ The probability of one boy and two girls is $\frac{3}{8}$ ----- (0/1 mark)

$$Q8(a) \sec 2\alpha + \tan 2\alpha = \frac{\cos \alpha + \sin \alpha}{\cos \alpha - \sin \alpha}$$

consider RHS

Rationalize
the denominator

$$\frac{\cos \alpha + \sin \alpha}{\cos \alpha - \sin \alpha} \times \frac{\cos \alpha + \sin \alpha}{\cos \alpha + \sin \alpha} \quad \text{--- (0.1 mark)}$$

$$\frac{\cos^2 \alpha + 2\cos \alpha \sin \alpha + \sin^2 \alpha}{\cos^2 \alpha - \sin^2 \alpha} \quad \text{--- (0.1 mark)}$$

$$\frac{1 + \sin 2\alpha}{\cos 2\alpha} \quad \text{--- (0.1 mark)}$$

$$= \frac{1}{\cos 2\alpha} + \frac{\sin 2\alpha}{\cos 2\alpha} \quad \text{--- (0.5 mark)}$$

$$= \sec 2\alpha + \tan 2\alpha \text{ proved (0.1 mark)}$$

(b)

$$\tan 2\alpha = 1$$

$$2\alpha = \tan^{-1}(1)$$

$$\frac{2\alpha}{2} = \frac{45^\circ}{2}$$

$$\alpha = \frac{45^\circ}{2}$$

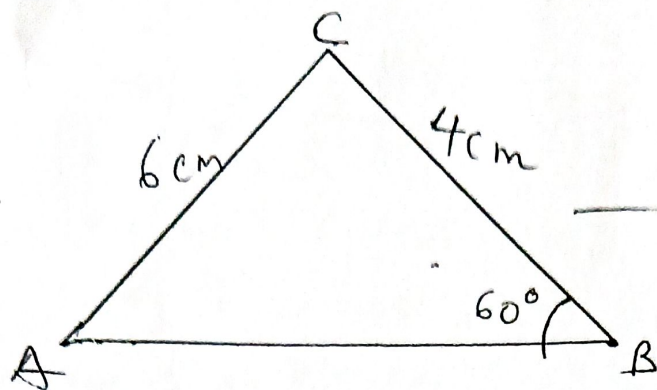
For tangent to be positive

$$360^\circ - \frac{45^\circ}{2}$$

$$337.5^\circ$$

$$\therefore 22.5^\circ \text{ and } 337.5^\circ$$

(0.1 mark)



(0/1 mark)

By sine rule

$$\frac{AC}{\sin B} = \frac{BC}{\sin A} \quad (0 \frac{1}{2} \text{ mark})$$

$$\frac{6\text{cm}}{\sin 60^\circ} = \frac{4\text{cm}}{\sin \theta} \quad (0/1 \text{ mark})$$

$$\frac{6\text{cm} \sin \theta}{6\text{cm}} = \frac{4\text{cm} \times \sin 60^\circ}{6\text{cm}} \quad (0 \frac{1}{2} \text{ mark})$$

$$\sin \theta = 0.5773$$

$$\theta = \sin^{-1}(0.5773)$$

$$\theta = 35^\circ$$

(0 0 1/2 mark)

09
i coordinate of A and B

At point A $y = 0$

$$y = \ln x$$

$$0 = \ln x$$

$$x = e^0$$

$$x = 1$$

$$A(1, 0)$$

(0/1 mark)

At point B

$$y = 2 \ln(x-6)$$

(0/1 mark)

(0/1 mark)

$$y = 2 \ln(x-6)$$

$$\frac{0}{2} = \frac{2}{2} \ln(x-6)$$

— (01 mark)

$$e^0 = x-6$$

$$x-6=1$$

$$x=7$$

$$B(7,0)$$

— (00 1/2 mark)

q(ii)

$$y = \ln x$$

$$y = 2 \ln(x-6)$$

$$\ln x = 2 \ln(x-6)$$

f 01 mark

$$\ln x = \ln(x-6)^2$$

$$x = (x-6)^2$$

$$x = x^2 - 12x + 36$$

$$x = 9$$

— (00 1/2 mark)

From $y = \ln x$

$$y = \ln 9$$

$$y = 2 \ln 3$$

$$C = (9, 2 \ln 3)$$

or
 $(9, 2.2)$

— (00 1/2 mark)

q(b)

$$9^x - 3^x - 6 = 0$$

$$(3^2)^x - 3^x - 6 = 0$$

$$(3^x)^2 - 3^x - 6 = 0$$

— (01 mark)

$$u = 3^x$$

— (00 1/2 mark)

$$u^2 - u - 6 = 0$$

$$u = 3 \text{ and } u = -2$$

$$3^x = 3$$

Apply log both sides

$$\log 3^x = \log 3$$

$$x \log 3 = \log 3$$

$$\log 3 \cdot \log 3$$

$$x = 1$$

(0/1 mark)

(0/1 mark)

soln

let x be number of adult tickets sold

y be the number of student tickets

z be number of children tickets

(0/1/2 mark)

$$x + y + z = 400$$

$$40x + 20y + 10z = 10600$$

(0/1/2 mark)

$$\text{Matrix } D \begin{bmatrix} 1 & 1 & 1 \\ 40 & 20 & 10 \\ 1 & 1 & -1 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \end{bmatrix} = \begin{bmatrix} 400 \\ 10600 \\ 200 \end{bmatrix}$$

(0/1/2 mark)

$$\text{Determinant of matrix } D \begin{bmatrix} 1 & 1 & 1 \\ 40 & 20 & 10 \\ 1 & 1 & -1 \end{bmatrix} = 40$$

$$D_x = \begin{bmatrix} 400 & 1 & 1 \\ 10600 & 20 & 10 \\ 200 & 1 & -1 \end{bmatrix}$$

$$\text{Determinant of } D_x = 700$$

(0/1/2 mark)

10(a) Determinant of Y from
$$\begin{bmatrix} 1 & 400 & 1 \\ 40 & 10600 & 10 \\ 1 & 1 & -1 \end{bmatrix} \quad \text{--- (0.5 mark)}$$

$$D_y = 4800$$

Determinant of Z
$$\begin{bmatrix} 1 & 1 & 400 \\ 40 & 20 & 10600 \\ 1 & 1 & 200 \end{bmatrix}$$

$$D_z = 4000 \quad \text{--- (0.5 mark)}$$

$$X = \frac{D_x}{D} = \frac{7200}{40} = 180 \quad \text{--- (0.5 mark)}$$

$$Y = \frac{D_y}{D} = \frac{4800}{40} = 120 \quad \text{--- (0.5 mark)}$$

$$Z = \frac{D_z}{D} = \frac{4000}{40} = 100 \quad \text{--- (0.5 mark)}$$

There are 180 adults, 120 students and 100 children in attendance. --- (0.5 mark)

10(b) Let X be units of food. --- (0.5 mark)
 Y be units of drinks. --- (0.5 mark)

	Food	Drinks	Minimum requirement
Vitamin B	2	4	8
Iron	5	10	60
Cost (Tsh)	2000	1600	

10 (b) Constraints

$$2x + 4y \geq 8$$

$$x + 2y \geq 4 \quad \text{--- (i) --- (00\frac{1}{2} \text{ mark})}$$

$$5x + 10y \geq 60$$

$$x + 2y \geq 12 \quad \text{--- (ii) --- (00\frac{1}{2} \text{ mark})}$$

$$x \geq 0, y \geq 0 \quad \text{--- (iii) --- (00\frac{1}{2} \text{ mark})}$$

$$\text{objective function, } f(x, y) = 2000x + 1600y \quad \text{--- (00\frac{1}{2} \text{ mark})}$$

Corner Point	$f(x, y) = 2000x + 1600y$	Minimize value.
A(0, 6)	$2000(0) + 1600(6)$	9600
B(12, 0)	$2000(12) + 1600(0)$	24000

--- (00\frac{1}{2} \text{ mark})

Optimum solution is (0, 6) with 9600/- --- (00\frac{1}{2} \text{ mark})

$\therefore$ 0 units of food and 6 units of drinks should be consumed in order to minimize cost of 9600/-

10(b): GRAPH OF LINEAR PROGRAMMING

Scale: 1 cm = 10 units
 1 cm = 1 unit

