

NJOMBE REGION
PRENATIONAR EXAMINATION 2024
PHYSICS II
MARKING SCHEME

Question 01

(i) The height of the blood column is quite large at the feet than that at the brain. likewise, the blood pressure in humans is greater at the feet than at the brain. 12 marks

(ii) Data given;

- density of glycerine = $1.3 \times 10^3 \text{ kg m}^{-3}$
- viscosity of glycerine = 0.83 Pa s
- length of the tube (L) = 1.5 m
- radius of the tube (r) = $1 \text{ cm} = 0.01 \text{ m}$
- mass of glycerine flowing per second (m) = $4.0 \times 10^{-3} \text{ kg s}^{-1}$

From

$$V = \frac{m}{\rho} = \frac{4.0 \times 10^{-3}}{1.3 \times 10^3} = 3.077 \times 10^{-6} \text{ m}^3 \text{ s}^{-1} \quad \text{--- 01 mark}$$

Now,

$$V = \frac{\pi r^4 \Delta p}{8 \eta L} \quad \text{--- 00/2 marks}$$

$$\Delta p = \frac{8 V \eta L}{\pi r^4}$$

$$\Delta p = \frac{8 \times 3.077 \times 10^{-6} \times 0.83 \times 1.5}{\pi \times (0.01)^4} \quad \text{--- 01 mark}$$

$$\Delta p = 975.52 \text{ Pa} \quad \text{--- 00/2 marks}$$

(b)(i) velocity head $h = \frac{v^2}{2g}$ 00/2 marks

$$v^2 = 2gh$$

$$v = \sqrt{2gh}$$

$$v = \sqrt{2 \times 9.8 \times 0.4} \quad \text{or}$$

$$v = \sqrt{2 \times 9.8 \times 0.4} = 2.80 \text{ cm s}^{-1} \quad \text{--- 00/2 marks}$$

1 (b) (ii) given; $p_1 = 3.5 \times 10^5 \text{ Nm}^{-2}$ (before opening pipe)
 $p_2 = 3 \times 10^5 \text{ Nm}^{-2}$ (on opening the valve)
 $v_1 = 0$ (velocity flow before opening the pipe)
 $v_2 = ?$ (velocity of flow on opening the pipe.)

For the flow of water along a horizontal pipe;

$$p_1 + \frac{1}{2} \rho v_1^2 = p_2 + \frac{1}{2} \rho v_2^2 \quad \text{--- 0.5 marks}$$

$$p_1 - p_2 = \frac{1}{2} \rho (v_2^2 - v_1^2)$$

$$p_1 - p_2 = \frac{1}{2} \rho (v_2^2 - 0^2) \quad \text{--- 0.5 marks}$$

$$p_1 - p_2 = \frac{1}{2} \rho v_2^2 \quad \text{--- 0.5 marks}$$

$$v_2^2 = \frac{2(p_1 - p_2)}{\rho}$$

$$v_2 = \sqrt{\frac{2(p_1 - p_2)}{\rho}} \quad \text{--- 0.5 marks}$$

$$v_2 = \sqrt{\frac{2(3.5 \times 10^5 - 3 \times 10^5)}{1000}} \quad \text{--- 0.1 mark}$$

$$v_2 = 10 \text{ ms}^{-1} \quad \text{--- 0.1 marks}$$

(c) let a_1 - be the cross section area at point p
 a_2 - be the cross section area at point q
 v_1 - be the velocity at point p
 v_2 - be the velocity at point q
 h_1 - be the height of the ends p
 h_2 - be the height of the ends q

Then $a_1 = 4 \times 10^{-3} \text{ m}^2$

$$a_2 = 8 \times 10^{-3} \text{ m}^2$$

$$h_1 = 2 \text{ m}$$

$$h_2 = 5 \text{ m}$$

$$v_1 = 1 \text{ ms}^{-1}$$

and density of the liquid ρ be 10^3 kg m^{-3} .

1 (c) According to the equation of continuity; we have:

$$a_1 v_1 = a_2 v_2$$

$$v_2 = \frac{a_1 v_1}{a_2} \quad \text{--- only marks}$$

$$v_2 = \frac{4 \times 10^{-3}}{8 \times 10^{-3}} \times 1 = 0.5 \text{ m s}^{-1} \quad \text{--- only marks}$$

If p_1 and p_2 are pressures at the ends P and Q , then according to Bernoulli's theorem.

$$p_1 + \frac{1}{2} \rho v_1^2 + \rho g h_1 = p_2 + \frac{1}{2} \rho v_2^2 + \rho g h_2 \quad \text{--- only marks}$$

Work done by the pressure forces per unit volume is

$(p_1 - p_2)$ from the equation above.

$$(p_1 - p_2) = \rho g (h_2 - h_1) + \frac{1}{2} \rho (v_2^2 - v_1^2) \quad \text{--- only marks}$$

$$(p_1 - p_2) = 10^3 \times 9.8 (5 - 2) + \frac{1}{2} \times 10^3 (0.5^2 - 1^2)$$

$$(p_1 - p_2) = 10^3 \times 9.8 (3) + \frac{1}{2} \times 10^3 (-0.75) \quad \text{--- only marks}$$

$$(p_1 - p_2) = 29400 - 375 \quad \text{--- only marks}$$

$$(p_1 - p_2) = 29025 \text{ J m}^{-3} \quad \text{--- only marks}$$

Work done by the gravity forces per unit volume is equal to $\rho g (h_2 - h_1)$.

$$\text{Work done by gravity force} = \rho g (h_2 - h_1) \quad \text{--- only marks}$$

$$= 10^3 \times 9.8 \times (5 - 2) \quad \text{--- only marks}$$

$$= 10^3 \times 9.8 \times 3$$

$$= 29400 \text{ J m}^{-3} \quad \text{--- only marks}$$

1

(d)(i) Due to the typical shape of the wings, the layers of the air (or the streamlines) above the wings come closer to each other. Due to this, velocity of the air above the wings increases (in accordance with the equation of continuity). Now the air above the wings possesses more kinetic energy; according to Bernoulli's equation, pressure energy and hence pressure above the wings will become smaller. Due to the difference in pressure above and below the wings, the wings get uplifted and help the aeroplane to rise up against gravity.

(ii) given - mass of a loaded Boeing aircraft = $3.3 \times 10^5 \text{ kg}$ (M)
 - Total area of the wings (A) = 500 m^2 .

Let p_1 be the pressure below the wings
 - p_2 be the pressure above the wings

Then uplift force (F) = $(p_1 - p_2) A$ ----- ok
 $mg = (p_1 - p_2) A$ ----- ok

$$(p_1 - p_2) = \frac{mg}{A}$$

$$(p_1 - p_2) = \frac{3.3 \times 10^5 \times 9.8}{500}$$

$$(p_1 - p_2) = 6.47 \times 10^3 \text{ Nm}^{-2}$$

Question 02 :

(a) (i) Examples of transverse waves

- Ripples produced on the surface of water when stone is dropped into it.
- waves produced in a rope at one end when the free end is turned up and down rapidly.
- waves in a stretched string of musical instrument when the string is plucked.

Examples of longitudinal waves.

- Sound waves travel through air in the form of longitudinal waves
- when a spring is alternately expanded and stretched longitudinal waves are set up.
- vibrations of air column in an open pipe are longitudinal

(ii) let L_1 and L_2 be the lengths of the closed pipe and open pipe respectively and f_1 and f_2 are their corresponding frequencies.

$$f_1 = \frac{v}{4L_1} \quad \text{and} \quad f_2 = \frac{v}{2L_2}$$

- The frequency of the third overtone of the closed pipe = $7f_1$

- The frequency of the first overtone for open pipe = $2f_2$

if is given that

$$7f_1 = 2f_2$$

$$7 \times \frac{v}{4L_1} = 2 \times \frac{v}{2L_2}$$

$$\frac{L_1}{L_2} = \frac{7}{4}$$

- 2 (b) (i) - The light sources should be coherent. They must ~~be~~ have zero or constant phase difference.
- The two light sources used to produce interference should emit the monochromatic light.
 - The amplitude of the waves that are interfering are equal.
 - The two light sources should be narrow.
 - The distance between the two light sources should be very small as compared to their distance from the screen.

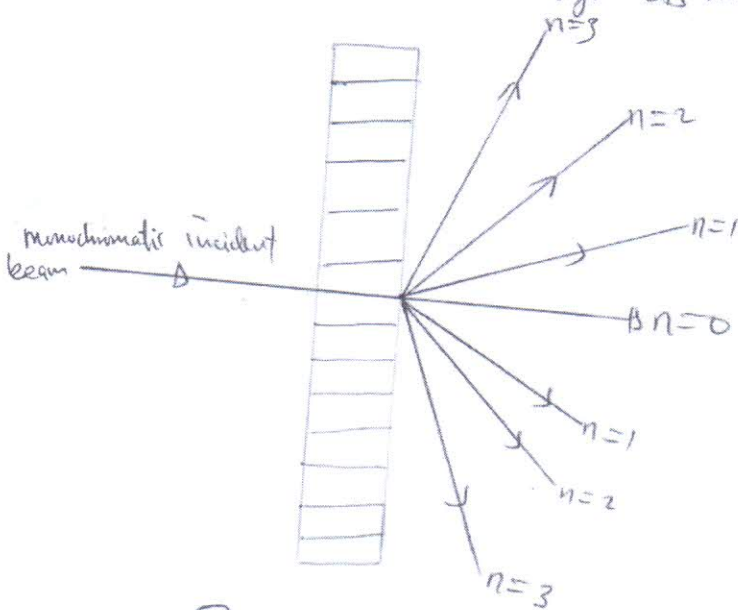
(ii) solution:

$$\sin \theta = \frac{n\lambda}{d}$$

$$\frac{n\lambda}{d} \leq 1$$

$$n \leq \frac{d}{\lambda} = \frac{2 \times 10^6}{600 \times 10^{-9}} = 3.33 \dots$$

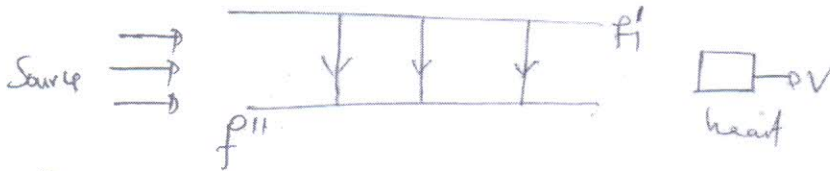
Since n must be an integer its maximum value is 3.



There are seven (7) diffracted beams. - (4 marks)

2 (c) (i) Doppler effect is an apparent change in observed frequency of a wave due to relative motions between the source and the observer. (01 mark)

(ii) Consider the figure below:



From $f' = \left(\frac{c-v}{c}\right) f$.

$\lambda' = \frac{c-v}{f'}$ and (01 mark)

$f'' = \frac{c}{\lambda'} = \left(\frac{c}{c+v}\right) f'$

but $\frac{c}{c+v} \cdot \frac{c-v}{c} f = f''$.

$f'' = \left(\frac{c-v}{c+v}\right) f$

$f'' = \frac{1.54 \times 10^3 - v}{1.54 \times 10^3 + v} \times 2.25 \times 10^6$ (01 mark)

but maximum beat frequency = $f - f''$

$2.25 \times 10^6 - 2.25 \times 10^6 \left(\frac{1.54 \times 10^3 - v}{1.54 \times 10^3 + v}\right) = 600$

on solving

maximum velocity $v = 0.205 \text{ m/s}$ on the surface of (01 mark)

2

(d) (i) when white light strikes the soap film, particular thickness of a film constructs or cancels particular colour of light by interference from the upper surface and that reflected from the reverse surface. If the thickness of the film cancels a colour of white light and its complementary colours appears. - 5 marks

(ii) ωt - phase angle with respect to time - - - - - 0.5 marks

kx - phase angle with respect to displacement - - - - - 0.5 marks

$(\omega t + kx)$ - phase angle of the wave - - - - - 0.5 marks

$\sin(\omega t + kx)$ - An oscillating term - - - - - 0.5 marks

Question 03.

(i) Ductile - A wire is said to be ductile, if the plastic region in the stress-strain graph is quite large.

(ii) Brittle - A wire is said to be brittle, if the plastic region in the stress-strain graph is quite small (practically zero).

(iii) Elastomers - The materials which can be greatly stretched

(iv) Elastic Fatigue - The loss of elastic strength of the material, caused due to repeated alternating strains to which the material is subjected.

(v) Elastic after effect - Is the delaying in regaining the original state by a body after the removal of deforming force.

01 @ = 5 marks

(b) given $a_1 = 1 \text{ mm}^2 = 10^{-6} \text{ m}^2$
 $a_2 = 2 \text{ mm}^2 = 2 \times 10^{-6} \text{ m}^2$

Suppose that the mass 'm' is suspended from a point C at a distance x from the end P of the rod.

As a result T_1 and T_2 be the tensions in the wire A and B respectively.

(i) when the stress is the same in the two wires

stress in the steel wire = $\frac{T_1}{a_1}$ - - - - - 0.5 marks

stress in the aluminium wire = $\frac{T_2}{a_2}$

3

(b) (i) Since the stress the two wires are equal.

$$\frac{T_1}{a_1} = \frac{T_2}{a_2} \quad \dots \dots \dots \text{00/2 marks}$$

$$\frac{T_1}{T_2} = \frac{a_1}{a_2} = \frac{10^{-6}}{2 \times 10^{-6}} = 0.5 \quad \dots \dots \dots \text{(i) } \dots \dots \dots \text{00/2 marks}$$

As suspended system of the rod and the two wires is in equilibrium.

$$T_1 \times PC = T_2 \times QC \quad \dots \dots \dots \text{00/2 marks}$$

$$T_1 x = T_2 (1.05 - x)$$

$$\frac{T_1}{T_2} = \frac{1.05 - x}{x} \quad \dots \dots \dots \text{(ii) } \dots \dots \dots \text{00/2 marks}$$

$$\frac{1.05 - x}{x} = 0.5 \quad \text{from eqn (i) and (ii) above.}$$

$$1.5x = 1.05$$

$$x = 0.7 \text{ m or } 70 \text{ cm from the steel wire } \dots \dots \dots \text{00/2 marks}$$

(ii) When the strain in the two wires are equal

Now; $\gamma = \frac{\text{stress}}{\text{strain}}$ or $\text{strain} = \frac{\text{stress}}{\gamma}$ \dots \dots \dots \text{00/2 marks}

Therefore, strain in the steel wire = $\frac{T_1/a_1}{\gamma_1} = \frac{T_1}{9171}$ \dots \dots \dots \text{00/2 marks}

Strain in the aluminium wire = $\frac{T_2/a_2}{\gamma_2} = \frac{T_2}{9272}$ \dots \dots \dots \text{00/2 marks}

Since the strains are equal in the two wires

$$\frac{T_1}{T_2} = \frac{9171}{9272} = \frac{10^{-6} \times 2 \times 10^{10}}{2 \times 10^{-6} \times 7 \times 10^{10}} = \frac{10}{7} \quad \dots \dots \dots \text{(i) } \dots \dots \dots \text{00/2 marks}$$

Again for the equilibrium of the system

$$T_1 PC = T_2 QC$$

$$T_1 x = T_2 (1.05 - x)$$

$$\frac{T_1}{T_2} = \frac{1.05 - x}{x} \quad \dots \dots \dots \text{(ii) } \dots \dots \dots \text{00/2 marks}$$

$$\frac{1.05 - x}{x} = \frac{10}{7} \quad \text{from eqn (i) and (ii) above.}$$

$$x = 0.432 \text{ m or } 43.2 \text{ cm } \quad \dots \dots \dots \text{00/2 marks}$$

$$X = 0.432 \text{ m or } 43.2 \text{ cm}$$

3 (c) (i) NO, stress is a scalar quantity. ----- 01 mark

(ii) Let h be the required depth of the sea.

$$\text{Now } K = \frac{P}{\frac{\Delta V}{V}} = \frac{\rho gh}{\frac{\Delta V}{V}} \text{ ----- 01 mark}$$

$$\text{here } \frac{\Delta V}{V} = 0.1\% = 0.001$$

$$K = 9.8 \times 10^8 \text{ Nm}^{-2}$$

$$\rho_{\text{sea}} = 10^3 \text{ kg m}^{-3}$$

$$\therefore 9.8 \times 10^8 = \frac{10^3 \times 9.8 \times h}{0.001} \text{ ----- 01 mark}$$

$$h = \frac{9.8 \times 10^8 \times 0.001}{10^3 \times 9.8}$$

$$h = 100 \text{ m} \text{ ----- 01 mark}$$

(d) (i) Surface energy = surface tension -----

(ii) Capillary action -----

(iii) let $r_1 = r$, Then $r_2 = \frac{r}{3}$.

Here $h_1 = 2 \text{ cm}$.

let h_2 - be the height, to which liquid rises in the second tube

$$\text{Now } h = \frac{2TC \cos \theta}{r \rho g}$$

or

$$h \propto \frac{1}{r} \text{ ----- 01 mark}$$

$$\frac{h_1}{h_2} = \frac{r_2}{r_1}$$

$$h_2 = \left(\frac{2r}{\frac{r}{3}} \right) = 6 \text{ cm} \text{ ----- 01 mark}$$

\therefore When the capillary tube is inclined: in the ascent formula, h refers to the vertical height of the liquid in the capillary tube. If the tube is inclined at an angle α with the vertical, then length of the tube is $\frac{h}{\sin \alpha}$.

(01 mark)

Question 04 :

(i) An electric field line - is the path along which a positive test charge would move if it is free to do so. ----- 01 mark

(ii) using the relation that:

$$E_r = \frac{E_m}{\epsilon_0} \quad \text{Then} \quad \epsilon_0 E_r = E_m$$

$$E = \frac{\phi}{4\pi\epsilon_0 r^2} = \frac{\phi}{4\pi\epsilon_0 \epsilon_r r^2} = \frac{k\phi}{\epsilon_r r^2} \quad \text{----- 01 mark}$$

$$E = \frac{9 \times 10^9 \text{ Nm}^2 \text{ C}^{-2} \times 3.3 \times 10^{-9}}{5 \times (10.0 \times 10^{-2})^2} \quad \text{----- 01 mark}$$

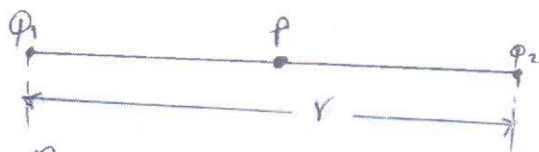
$$E = 594 \text{ N C}^{-1}$$

\therefore The electric field intensity $(E) = 594 \text{ N C}^{-1}$ ----- 01 mark

(b) (i) Electrostatic potential - is equal to the work done in bringing a positive charge from infinity to that point. ----- 01 mark

or
Is the potential energy per unit charge.

(ii)



by using the principle of superposition of electric potentials;

$$V_p = V_{\phi_1} + V_{\phi_2} \quad \text{----- 01 mark}$$

$$V_p = \frac{k\phi_1}{r/2} + \frac{k\phi_2}{r/2}$$

$$\text{hence } V_p = \frac{2k}{r} (\phi_1 + \phi_2) \quad \text{----- 01 mark}$$

$$V_p = \frac{2 \times 9 \times 10^9 \text{ Nm}^2 \text{ C}^{-2}}{20 \times 10^{-2} \text{ m}} \times (20 \times 10^{-6} \text{ C} + -20 \times 10^{-6} \text{ C})$$

$$V_p = 0 \text{ V} \quad \text{----- 01 mark}$$

Electrostatic potential at a point midway is 0V.

4 (c) (i) → surface area - from $C = \frac{A\epsilon_0}{d}$

Thus capacitance of a capacitor increases as the surface area increases.

→ distance between the plates - from $C = \frac{A\epsilon_0}{d}$

Thus capacitance of a capacitor is inversely proportional to the distance between the plates.

→ dielectric material - from $C = \frac{A\epsilon_0}{d}$

Thus capacitance of a capacitor is direct proportional to the dielectric constant of the material used between the plates.

(ii) from equation of the capacitance above:

$$C = \frac{A\epsilon_0}{d}$$

$C_0 = \frac{A\epsilon_0}{d}$; the capacitance with no dielectric material is;

$$C_0 = \frac{8.854 \times 10^{-12} \text{ C}^2 \text{ V}^{-1} \text{ m}^{-2} \times 100 \times 10^{-4} \text{ m}^2}{1.0 \times 10^{-3} \text{ m}}$$

$$C_0 = 8.854 \times 10^{-11} \text{ F}$$

The capacitance with dielectric material;

$$C = \frac{Q}{V} = \frac{0.12 \times 10^{-6} \text{ C}}{120 \text{ V}} = 1.0 \times 10^{-9} \text{ F}$$

The dielectric constant is;

$$\epsilon_r = \frac{C}{C_0} = \frac{1.0 \times 10^{-9} \text{ F}}{8.854 \times 10^{-11} \text{ F}} = 11.3$$

Therefore, the dielectric constant of the material is 11.3.

4 (d) (i) If two equipotential surfaces could intersect; then at the point of intersection there would be two values of electric potential which is not possible. --- 02 marks

(ii) work done = charge \times potential difference --- 01 mark
= $q \times (V_B - V_A)$
= $q \times 0$ since $V_A = V_B$ over equipotential surface.
= $0V$ --- 01 mark

by letting V_A and V_B be the potentials at point A and point B within the equipotential surfaces.

Thus there is no work done in moving a test charge within the equipotential surfaces.

(iii) - Electric potential due to point charge, $V \propto \frac{1}{r}$ while for dipole, $V \propto \frac{1}{r^2}$.

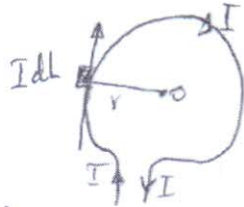
only 2 points - The potential due to dipole is axially symmetry while potential due to a point charge is spherically symmetric.

- The potential due to dipole not only depends on 'r' but also on the angle between the position vector \vec{r} and dipole moment vector \vec{p} . --- 01 mark @ 2 marks.

Question 05 :

(i) Biot-savart law states that "The magnetic field dB at point P at a distance r from a small current element $I dl$ of a conductor carrying current is given by; $dB \propto \frac{I dl \sin \alpha}{r^2}$ where α is the angle between \vec{dl} and \vec{r} . ----- 02 marks.

Consider the conductor in a circular shape below:



From Biot-savart law

$$dB \propto \frac{I dl \sin \alpha}{r^2}$$

$$dB = \frac{k I dl \sin \alpha}{r^2}, \text{ where } k = \frac{\mu_0}{4\pi} \text{ ----- } \frac{1}{2} \text{ marks}$$

$$dB = \frac{\mu_0 I dl \sin \alpha}{4\pi r^2}$$

$$\int dB = \frac{\mu_0 I \sin \alpha}{4\pi r^2} \int dl$$

where $\alpha = 90^\circ$ ----- $\frac{1}{2}$ marks

$$B = \frac{\mu_0 I \sin 90^\circ L}{4\pi r^2},$$

where $L = 2\pi r =$ circumference of the circular coil.

$$B = \frac{\mu_0 I \cdot 2\pi r}{4\pi r^2}$$

where $\sin 90^\circ = 1$ ----- $\frac{1}{2}$ marks

$$B = \frac{\mu_0 I}{2r}$$

\therefore The magnetic field at the centre is $\frac{\mu_0 I}{2r}$ ----- $\frac{1}{2}$ marks.

5 @ (ii) given; - radius $r = 0.5 \text{ nm}$
 - speed $v = 4 \times 10^6 \text{ m/s}$.

Required B .

from $B = \frac{\mu_0 I}{2r}$ but $I = \frac{e}{t}$ --- 01 mark

$$B = \frac{\mu_0 e}{2rt}$$

Also $t = \frac{2\pi r}{v} = \frac{2\pi \times 5 \times 10^{-10}}{4 \times 10^6}$

$t = 7.85 \times 10^{-16} \text{ seconds}$ --- 01 mark

$$B = \frac{4\pi \times 10^{-7} \times 1.6 \times 10^{-19}}{2 \times 0.5 \times 10^{-9} \times 7.85 \times 10^{-16}}$$

$B = 0.256 \text{ T}$ --- 01 mark

\therefore Thus the magnetic field at the centre is 0.256 T .

(b) (i) One ampere is the current flowing in each of the two infinitely long parallel conductors 1 m apart, which result in a force of exactly $2 \times 10^{-7} \text{ N}$ per metre length of each conductor. --- 02 marks

(ii) The rule is Fleming's left hand rule which states that "stretch the fore finger, middle finger and thumb of your left hand in mutually perpendicular directions, If the fore finger points in the direction of current, then the thumb gives the direction of the force on the conductor".

- right hand rule can also be used. --- 02 marks.

(c) given $I_1 = 4 \text{ A}$, $I_2 = 6 \text{ A}$, $r = 3 \text{ cm} = 3 \times 10^{-2} \text{ m}$,

required F/L of the straight long conductor carrying current.

$$F/L = f = \frac{\mu_0 I_1 I_2}{2\pi r}$$
 --- 01 mark

$$f = \frac{4\pi \times 10^{-7} \times 4 \times 6}{2\pi \times 3 \times 10^{-2}}$$
 --- 01 mark

$f = 1.6 \times 10^{-4} \text{ N/m}$. --- 01 mark

Since the currents are in opposite direction, then the force is repulsive which means that the conductor of 4 A will be pushed away.

5 (a) (i) Faraday's law of electromagnetic induction states that "Whenever the magnetic flux linking the conductor or coil changes an emf is induced in a conductor or coil which is directly proportional to the rate of flux linkages." - - - - - 02 marks

$$\text{Thus emf } \epsilon \propto N \frac{d\phi}{dt}$$

- (ii) - The change of magnetic flux density -
 - The change of the area (A) of the coil 01 @ = 3 marks.
 - The change of the orientation of the coil

Question 06.

(a) (i) The activity of a radioactive decay is the rate of disintegration of radioactive substance. - - - - - 01 mark

(ii) From $\frac{dN}{dt} = -\lambda N$. - - - - - 00 1/2 marks

$$\frac{dN}{N} = -\lambda dt \quad \text{integrate both sides}$$

$$\int_{N_0}^N \frac{dN}{N} = -\lambda \int_0^t dt \quad \text{--- --- --- 00 1/2 marks}$$

$$[\ln N]_{N_0}^N = -\lambda(t-0)$$

$$\ln\left(\frac{N}{N_0}\right) = -\lambda t$$

$$\frac{N}{N_0} = e^{-\lambda t}$$

$$N = N_0 e^{-\lambda t} \quad \text{--- --- --- 00 1/2 marks}$$

when $t = t_{1/2}$, $N = N_0/2$

Then

$$\frac{N_0}{2} = N_0 e^{-\lambda t_{1/2}} \quad \text{--- --- --- 00 1/2 marks}$$

$$\frac{1}{2} = e^{-\lambda t_{1/2}}$$

$$\ln\left(\frac{1}{2}\right) = \ln e^{-\lambda t_{1/2}}$$

$$\ln 2^{-1} = -\lambda t_{1/2} \ln e \quad \text{--- --- --- 00 1/2 marks}$$

$$-\ln 2 = -\lambda t_{1/2}$$

$$\ln 2 = \lambda t_{1/2}$$

00 1/2 marks

6 @ (iii) Given that; Half life $t_{1/2} = 5.3 \text{ years}$

Activity (A) = $1 \times 10^3 \text{ Ci}$

mass (m) = ?

$A = 1 \times 10^3 \times 3.7 \times 10^{10} \text{ dis/s (Bq)}$ --- 0.5 marks

$t_{1/2} = (5.3 \times 365 \times 24 \times 3600) \text{ seconds}$ --- 0.5 marks

But $A = \frac{\ln 2}{t_{1/2}} \cdot N$ --- 0.5 marks

$N = \frac{1 \times 10^3 \times 3.7 \times 10^{10} \times 5.3 \times 365 \times 24 \times 3600}{0.693}$ --- 0.5 marks

$N = 8.92 \times 10^{15} \text{ atoms}$

but $n = \frac{N}{N_A} = \frac{8.92 \times 10^{15}}{6 \times 10^{23}} = 1.486 \times 10^{-8} \text{ mol}$

$\therefore n = 1.486 \times 10^{-8} \text{ mol}$ --- 0.5 marks

Again $n = \frac{\text{Mass}}{\text{Molar mass (Mv)}}$

Mass = $n \times Mv = 1.486 \times 10^{-8} \text{ mol} \times 605 \text{ mol}^{-1} \text{ g}$

Mass = $8.92 \times 10^{-7} \text{ g}$ --- 0.5 marks

(b) (i) The negative total energy means that an electron is bound to the nucleus. --- 0.5 marks

(ii) Rutherford's model

- electrons can revolve around the nucleus in any orbit
- Electrons lose energy continuously and hence produce continuous spectrum

Bohr's model.

- electrons can revolve around the nucleus in orbit of definite radii
- Electrons emit radiation only when it makes a sudden change from one energy state to another energy state.

0.5 marks

(iii) The magnitude of energy of electron in the first orbit of hydrogen atom is

$E_1 = \frac{me^4}{8h^2\epsilon_0^2}$ --- 0.5 marks

6 (b) (iii)

$$hf = \frac{me^4}{8\epsilon_0^2 h^2} \quad \text{--- --- --- } \text{1/2 marks}$$

$$f = \frac{me^4}{8\epsilon_0^2 h^3}$$

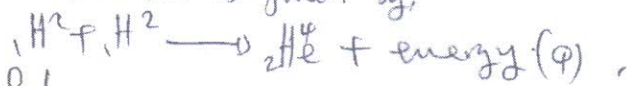
$$T = \frac{1}{f} = \frac{8\epsilon_0^2 h^3}{me^4} \quad \text{--- --- --- } \text{1/2 marks}$$

$$T = \frac{8 \times (8.85 \times 10^{-12})^2 \times (6.62 \times 10^{-34})^3}{9.1 \times 10^{-31} \times (1.6 \times 10^{-19})^4} \quad \text{--- --- --- } \text{1 mark}$$

$$T = 0.305 \times 10^{-15} \text{ seconds} \quad \text{--- --- --- } \text{1/2 marks}$$

(c) (i) The mass of the nucleus is always less than the sum of the masses of its constituents protons and neutrons. The mass difference (energy) hold the nucleus together and is called the total binding energy. --- --- --- 02 marks

(ii) The fusion reaction is given by;



$$\text{Mass defect } \Delta m = (2 \times 2.0141) - 4.0026$$

$$\Delta m = 0.0256 \text{ a.m.u.} \quad \text{--- --- --- } \text{1/2 marks}$$

1 a.m.u = 931 MeV, the energy released in the reaction is

$$\phi = 0.0256 \times 931 = 23.833 \text{ MeV} \quad \text{--- --- --- } \text{1/2 marks}$$

Useful energy available per reaction. --- --- --- 1/2 marks

$$= 25\% \text{ of } \phi$$

$$= 0.25 \times 23.833$$

$$= 5.9582 \text{ MeV}$$

$$= 5.9582 \times 10^6 \times 1.6 \times 10^{-19} \text{ J}$$

$$= 9.533 \times 10^{-13} \text{ J} \quad \text{--- --- --- } \text{1/2 marks}$$

Energy obtained per day;

$$= 200 \times 10^6 \times 24 \times 60 \times 60$$

6 (c) (ii) Mass of deuterium fuel needed for reaction
 $= 2 \times 2.0141 = 4.0282 \text{ g.m.u.}$ --- 0.5 mark

Now: $\frac{4.0282}{6.02 \times 10^{23}} = 0.6691 \times 10^{-23} \text{ g}$ --- 0.1 mark

Mass of deuterium required per day.

$$= \frac{0.6691 \times 10^{-23} \times 1.728 \times 10^{13}}{9.533 \times 10^{-13}} \text{ --- 0.5 mark}$$

$$= 121.3 \text{ g} \text{ --- 0.5 mark}$$